

# Comparative Analysis of OFDM PAPR using SLM & PTS Techniques

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**ABSTRACT:** *New technology in communication system emerged as MIMO-OFDM(Orthogonal frequency division multiplexing) innovation is standout amongst the most alluring contender for fourth generation (4G) mobile radio communication. It is the most up and coming & most recent innovation utilised as a form of ADSL, Digital audio broadcasting, and HiperLAN network. It is a strategy for transmitting data simultaneously over different similarly separated carrier frequency using Fourier transform. It successfully combats the multipath fading channel and improves the bandwidth efficiency. In the mean time, it also enhances the system capacity so as to give a reliable transmission.*

*The fundamental downside of a MIMO-OFDM system is a high peak-to-average power ratio (PAPR) for a large number of sub-carriers, which result in numerous confinements for useful applications.*

*A few methods have been utilized to reduce the PAPR. Some of these techniques are Coding, phase rotation and clipping are among one of the leading PAPR reduction schemes that have been proposed to overcome this problem. In this dissertation, we will lessen the peak to average power ratio i.e. PAPR by actualizing the selected mapping technique and partial transmit technique and then compare the result with original OFDM and both of selected mapping technique and partial transmit technique.*

**Keywords:** *Multiple Input Multiple Output (MIMO), Orthogonal Frequency Division Multiplexing (OFDM), Peak-To-Average Power Ratio (PAPR), Selected Mapping (SLM), Partial Transmit Sequence (PTS).*

## 1. Introduction

Marconi is a first person to explore new field of the wireless industry more than 100 years back. Today life does not appear conceivable without wireless in some structure or the other. Wireless communication is one of the quickest developing commercial ventures [1, 2, 3]. It penetrates each part of our lives. Later progresses in wireless communication systems have expanded the throughput over wireless channels; furthermore the dependability of wireless communication systems has been expanded. The fundamental main impetus behind the quick improvement of wireless communication systems is the guarantee of compactness, portability, and availability. Wired communication is steadier and exceedingly dependable, yet limits the clients to a limited domain. Sensibly, individuals pick flexibility versus restriction. Hence, there is a characteristic inclination towards disposing of wires if conceivable. While, this flexibility is the primary main aim for clients, the punishment for this flexibility is frequently lower quality, protection, security, or lower throughput contrasted with the proportionate wired arrangement. The requests on bandwidth and spectral availability are likewise







needing Channel Side Information(CSI). Tone reservation scheme is to chose the frequency-domain reserved-subcarriers as cancellation signal such that it minimizes the PAPR. At the receiver, the tone-reserved subcarriers can be discarded at the receiver without CSI, TR is computationally simple, but might violate some standards. Tone injection requires much complexity at the transmitter by substituting a point in the basic constellation for a new point in the extended constellation, thus wont be adopted on the handset uplink.

Several PAPR reduction techniques based on PTS or SLM schemes without requirement of side information are also introduced. Alavi [20] derives a simplified maximum likelihood (ML) decoder for SLM and PTS that operates without side information. The proposed SLM and PTS systems are not supposed to lose throughput due to side information or decrease bit error rate due to errors inside information. However, a decrease in throughput occurs because of the pilot tones utilised for channel estimation.

### 3. Orthogonal Frequency Division Multiplexing

Orthogonal Frequency Division Multiplexing (OFDM) is generalised as a type of multi-carrier modulation where the carrier spacing is precisely chosen with the goal that every sub carrier is orthogonal to the next sub carrier. Two signs are orthogonal if they show zero dot product. That is,

whether you take two signals increase them together and if their integrtion over an interim is zero, then two signs are orthogonal in that interim. Orthogonality can be accomplished via deliberately selecting carrier separation, for example, letting the carrier dispersing be equivalent to the complementary of the helpful symbol period. As the sub carriers are orthogonal, the range of every carrier has an invalid at the inside frequency of each of alternate carriers in the system. This outcomes in no obstruction between the carriers, permitting them to be dispersed as close as hypothetically conceivable. The real points of interest of OFDM are its capacity to change over a frequency specific blurring channel into a few almost level blurring channels and high ghostly productivity. In any case, one of the principle impediments of OFDM is its affectability against carrier frequency counterbalance which causes constriction and revolution of subcarriers, and Inter channel interference (ICI). The undesired ICI corrupts the execution of the system.

In OFDM, the different frequency channels, known as sub-carriers, are orthogonal to one another. A surely understood issue of OFDM, be that as it may, is its affectability to frequency balance between the transmitted and received signals, which might be brought on by Doppler movement in the channel, or by the distinction between the transmitter and receiver

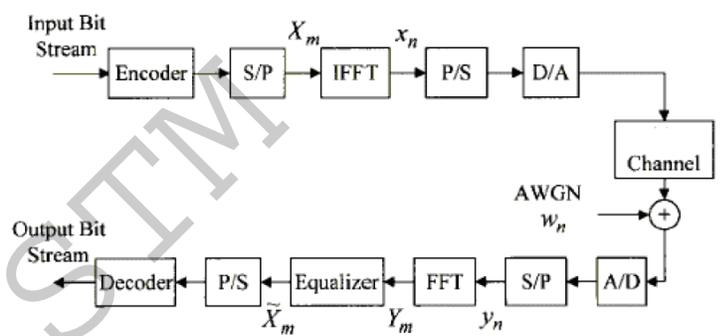
nearby oscillator frequencies. This carriers frequency counterbalance causes loss of orthogonality between sub-carriers and the signals transmitted on every carrier are not autonomous of one another, prompting between carrier obstruction (ICI).

The Orthogonality among the carriers can be kept up if the OFDM signal is characterized by utilizing Fourier transform methods. The OFDM system transmits a substantial number of narrowband carriers, which are firmly divided. Note that at the focal frequency of the every sub channel there is no crosstalk from other sub channels. In an OFDM system, the information bit stream is multiplexed into N signal streams, each with signal period  $T_s$ , and every signal stream is utilized to adjust parallel, synchronous sub-carriers. The sub-carriers are divided by  $1/NT_s$  in frequency, in this way they are orthogonal over the interim  $(0, T_s)$ . A common discrete-time baseband OFDM handset system is appeared in Figure 1. Initial, a serial-to-parallel (S/P) converter gatherings the surge of information bits from the source encoder into gatherings of  $\log_2 M$  bits, where M is the letter set of size of the advanced regulation signal utilized on every sub-carrier. A sum of N such signals,  $X_m$ , are made. At that point, the N signals are mapped to receptacles of an opposite quick Fourier change (IFFT). These IFFT containers relate to the orthogonal sub-carriers

in the OFDM signal. Thusly, the OFDM signal can be communicated as

$$x(n) = \frac{1}{N} \sum_{m=0}^{N-1} X_m e^{j \frac{2\pi mn}{N}} \quad 0 \leq n \leq N-1 \quad 1$$

Where  $X_m$  are the baseband signals on every sub-carriers. The computerized to-simple (D/A) converter then makes a simple time-area signal which is transmitted through the channel.



**Fig.1: Baseband OFDM transceiver system.**

At the receiver, the signal is changed over back to a discrete N point arrangement  $y(n)$ , relating to every sub-carriers. This discrete sign is demodulated utilizing a N-point quick Fourier change (FFT) operation at the receiver. The demodulated signal stream is given by:

$$Y(m) = \sum_{n=0}^{N-1} y(n) e^{-j \frac{2\pi mn}{N}} + W(m) \quad 0 \leq m \leq N-1 \quad 2$$

Where  $W(m)$  relates to the FFT of the examples of  $w(n)$ , which is the Additive White Gaussian Noise (AWGN) presented in the channel. The rapid information rates for OFDM are expert by the concurrent transmission of information at a lower



rate on each of the orthogonal sub-carriers. On account of the low information rate transmission, twisting in the got signal impelled by multi-way postpone in the channel is not as critical when contrasted with single-carrier high-information rate systems. For instance, a narrowband signal sent at a high information rate through a multipath channel will encounter more prominent negative impacts of the multipath delay spread, in light of the fact that the signals are much closer together. Multipath contortion can likewise bring about between signal impedance (ISI) where nearby signals cover with one another. This is averted in OFDM by the insertion of a cyclic prefix between progressive OFDM signals. This cyclic prefix is disposed of at the receiver to counterbalance ISI. It is because of the vigor of OFDM to ISI and multipath bending that it has been considered for different remote applications and models.

#### 4. PAPR REDUCTION & ITS TECHNIQUES

In above section, we talked about fundamental principles of OFDM and demonstrated how it is a useful innovation for the up and coming era of high information rate correspondence systems. However a few configuration issues should be tended to, a standout amongst the most essential being the Peak to Average Power Ratio (PAPR) of the profoundly fluctuating transmit signal envelope. Because of the way of the IFFT, it wholes N sinusoids through superposition, a few mixes of the sinusoids make

expansive peaks. The disadvantage of an expansive element reach is that it places weight on the outline of parts, for example, the word length of the IFFT/FFT pair, DAC and ADC, blender stages, and in particular the HPA which must be intended to handle sporadically happening expansive tops. Inability to outline segments with an adequately extensive direct range results in immersion of the HPA. Immersion makes both in band mutilation, expanding the BER and out of band bending, or ghastly splatter, which causes ACI. One clear arrangement is to plan the parts to work inside vast direct districts, in any case this is unrealistic as the segments will work wastefully and the expense turns out to be restrictively high. This is particularly evident in the HPA where a significant part of the expense and ~50% of the span of a transmitter lies.

#### 4.1 Peak to Average Power Ratio

The PAPR is the ratio between the maximum power of a sample in a given OFDM transmit symbol separated by the average power of that OFDM symbol. The mean envelope power of the baseband expression (expecting same heavenly body on each subcarrier) is characterized as

$$P = \frac{1}{T} \int_{t=0}^T |x_m(t)|^2 dt = \frac{1}{N} \sum_{k=0}^{N-1} |X_{m,k}|^2 \quad 3$$

$X_{m,k}$  are assumed to be complex Quadrature Amplitude Modulated (QAM) data which are statistically independent, identically distributed



(i.i.d) random variables with 0 mean and variance.

The average power is defined as

$$P_{av} = E[P] = E\left[|x_m(t)|^2\right]$$

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The problem with OFDM is that theoretically the PAPR can be up to  $\log_2(N)$ , which is huge.

#### 4.2 PAPR Reduction Techniques

There are a wide range of calculations that have been proposed to take care of the high PAPR issue of OFDM system. These decrease arrangements can be generally separated into three classifications:

##### 1. Signal Distortion

A standout amongst the most down to earth and simplest methodologies is clipping and filtering which can clip the sign at the transmitter in order to dispense with the presence of high tops over a specific level. Section can be executed to the discrete specimens preceding digital to analog convertor (DAC) or by outlining digital to analog convertor (DAC) and/or enhancer with immersion levels which are lower than the dynamic extent. Be that as it may, because of the nonlinear mutilation presented by this procedure, orthogonality will be decimated to some degree which results in genuine in band commotion and out of band noise. In-band noise can't be evacuated by separating, it diminishes the bit error rate (BER). Out-of-band noise diminishes the data transfer capacity effectiveness yet frequency area sifting can be utilized to

minimize the out-of-band force. In spite of the fact that sifting goodly affects commotion concealment, it might bring about peak re-development. To conquer this downside, the entire procedure is rehashed a few times until a fancied circumstance is accomplished. Besides, some other novel proposition which consolidate this strategy with coding and/or signal scrambling have as of now been concentrated on by other scientist.

##### 2. Signal Scrambling Techniques

The crucial guideline of this method is to scramble each OFDM signal with various scrambling successions and select one which has the littlest PAPR esteem for transmission. Evidently, this procedure does not ensure diminishment of PAPR quality underneath to a specific edge, however it can decrease the appearance probability of high PAPR all things considered. This kind of methodology include: Selective Mapping (SLM) and Partial Transmit Sequences (PTS). SLM strategy applies scrambling revolution to all sub-carriers autonomously while PTS technique just takes scrambling to part of the sub-carriers. These two strategies can be connected to any situations without confinement on the quantity of sub-carriers and kind of balance. In any case, for effective recuperation of the sign at the collector, extra data is required. That prompts low transmission capacity use and high equipment intricacy for execution.

##### 3. Coding Techniques



The center of encoding strategy is to apply exceptional forward mistake adjustment method to evacuate the OFDM signals with high PAPR. The traditional plans incorporate direct square code, Golay codes and Reed-Muller code. To the extent straight piece code technique is concerned, it is just reasonable to the situation which has a little number of sub-carriers, which results in restricted applications. Reed-Muller code is a high proficiency coding plan, it acquires a lower PAPR for the second request cosets code by ordering the Walsh-Hadamard change (WHT) range of the code words. By utilizing Reed-Muller code, PAPR can be decreased to 3dB at most with a decent blunder redressing execution. Be that as it may, with everything taken into account, the encoding strategy is constrained to sorts of group of constellations.

##### 5. Proposed Methodology for SLM Scheme

In this section, an assessment of elements which could impact the PAPR reduction execution is performed utilizing MATLAB. Taking into account the standards of SLM calculation, it is evidently that the capacity of PAPR diminishment utilizing SLM is influenced by the course number  $M$  and subcarrier number  $N$ . In this manner, simulations with various  $M$ 's value and  $N$ 's value will be taken, and the outcomes show some wanted properties of signal related to the same data [21].

1. Examination of performance of PAPR reduction with various estimations of  $M$  while  $N$  is settled at 128:

Firstly from the points of view of unpredictability and practicability, revolution variable is characterized as  $\in [\pm 1, \pm j]$ . This diminishes count unpredictability significantly contrasted with performing random complex duplication. The calculation executes 10000 times, over-examining component is 8 and QPSK mapping is received as regulation plan in every sub-transporter. Course numbers  $M=2$ ,  $M=4$ ,  $M=8$ ,  $M=16$  and  $M=32$  are utilized. The likelihood of high PAPR is fundamentally diminished. Expanding  $M$  prompts the change of PAPR reduction execution. In the event that the likelihood is set to 1% and afterward the CCDF bends with various  $M$  qualities are looked at. The PAPR estimation of case  $M=2$  is around 1dB littler than the unmodified one  $M=1$ . Under the same condition, the PAPR estimation of case  $M=16$  is around 3dB littler than the first one  $M=1$ . Be that as it may, from the correlation of the bend  $M=8$  and  $M=16$ , we discovered that the execution contrast between these two cases is under 0.5dB. Examination of PAPR diminishment execution with various  $N$  values while  $M$  is settled at 8:

For this situation, we set the quantity of OFDM sign edge  $M$  equivalent to 8, the quantity of subcarrier  $N$  equivalent to 256, 128, and 64, separately. Result appeared in next figure, the CCDF bend of unique

successions PAPR is given as the reference of correlation with the others which SLM technique been utilized. Result appeared in next assume that SLM calculation especially appropriate for the OFDM situation with bigger number of sub-carriers.

### 6. Proposed Methodology for PTS Scheme

We understood from the above exchange that in PTS approach, there are differing parameters affect the PAPR diminishment execution, these are: 1) The quantity of sub-squares  $V$ , which impacts the multifaceted nature firmly; 2) The quantity of conceivable stage esteem  $W$ , which affects the many-sided quality too; and 3) The sub-piece segment plans. In our recreation, two parameters will be considered. They are sub-square sizes  $V$  and diverse sub-piece parcel proposition.

1. PAPR diminishment execution impacts by number of sub-squares  $V$ :

Reenactment assesses the PAPR diminishment execution utilizing PTS calculation with various  $V$ , in which reenactment design, QPSK is connected,  $N = 256$  and  $V = 0, 2, 3, 4$ , individually.

2. PAPR diminishment execution impacts by various quality reach  $W$ :

The reproduction result in next chapter which demonstrates the fluctuating PAPR reduction execution with various  $W$  (gathering scope of weighting component) when utilizing PTS diminishment plan. Recreation particular parameters are: the quantity of sub-transporters  $N = 128$ , QPSK

$v$  heavenly body balance, oversampling variable takes  $L = 8$ , the quantity of sub-piece  $V = 4$ , CCDF bend has almost 1dB change when  $W = 4$ , contrasted with  $W = 2$ , the 1% PAPR is around 7.5 dB. We reason that in a PTS-OFDM framework, the bigger  $W$  esteem takes, the better PAPR execution will be gotten when the quantity of sub-square  $V$  is settled.

## 7. Simulation Results

### 7.1 Simulations result using SLM Technique

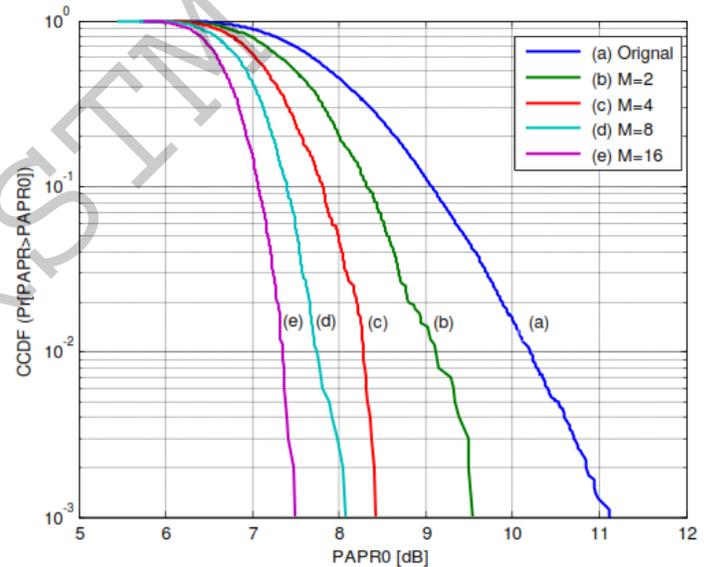


Fig. 2: PAPR comparison using different values of  $M$

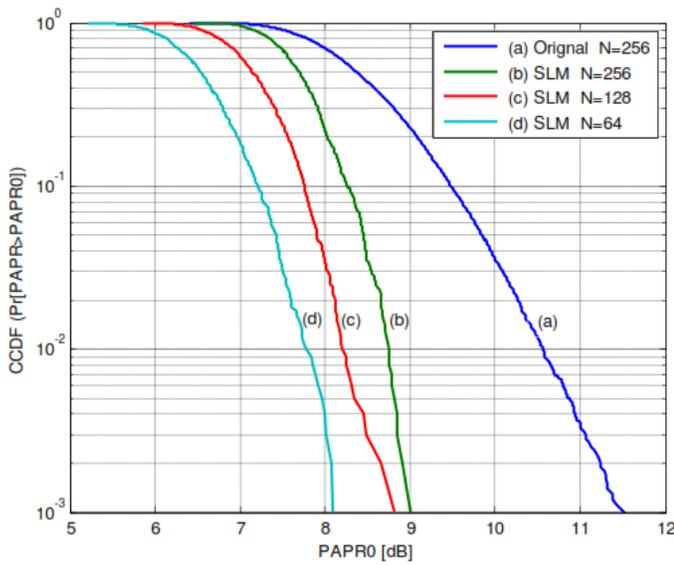


Fig. 3: PAPR comparison using different values of  $N$ .

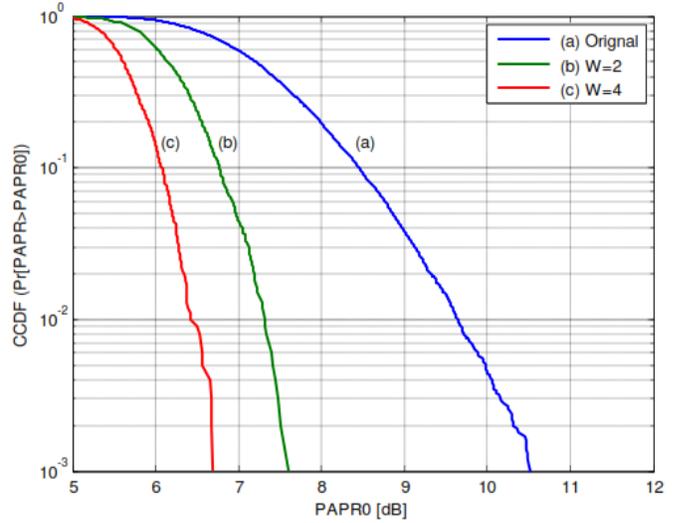


Fig. 5: PAPR comparison using different values of  $W$ .

### 7.2 Simulation result using PTS Technique

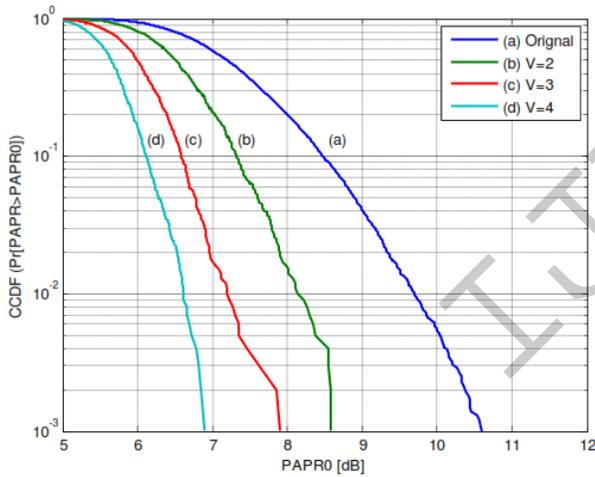


Fig. 4: PAPR comparison using different values of  $V$ .

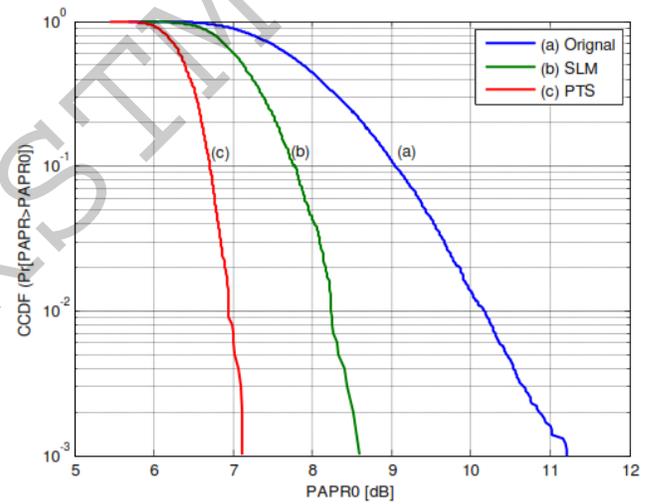


Fig. 6: PAPR comparison using performances between PTS algorithm and SLM algorithm for PTS-OFDM system.

It demonstrates plainly that PTS technique gives a superior PAPR lessening execution contrasted with SLM strategy. By the by, the expense is additionally paid for yielding transmission productivity and rising many-sided quality. In this way, in down to earth applications, a tradeoff ought to be made between great execution and assistant data. From the



talk above, we can say that SLM calculation is more reasonable if system can endure more excess data, generally, PTS calculation is more worthy when many-sided quality turns into the main considering element. In a word, trade off will be made for a solid system.

### 7. Conclusion

In this paper, we have compared the two PAPR reduction techniques known as SLM & PTS. Results are satisfactory as per theory and also it is concluded that PTS gives much better PAPR reduction as compare to SLM technique.

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